

**Çankaya University**  
**Electrical & Electronics Engineering Department**  
**EE 465 Power Systems**  
**Midterm Exam 1**

**90 mins**

**Q1-(35)** A three-phase line with an impedance of  $(0.2+j1) \Omega/\text{phase}$  feeds three balanced three-phase loads connected in parallel.

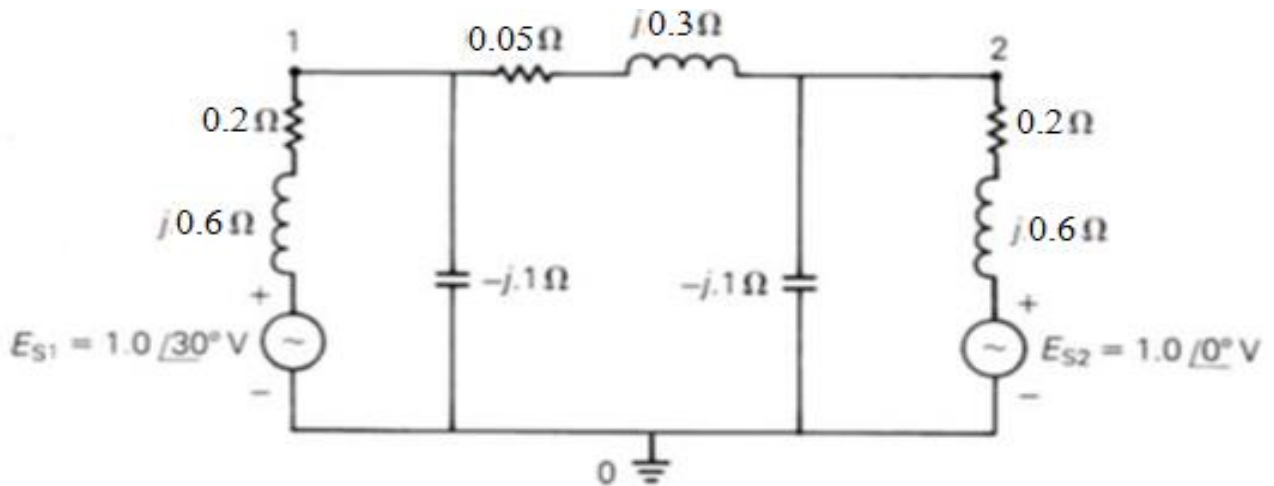
**Load 1:** Is an inductive load with 150 kW and 120 kvar

**Load 2:** Delta connected capacitive load with an impedance of  $(150 -j48) \Omega/\text{phase}$ ,

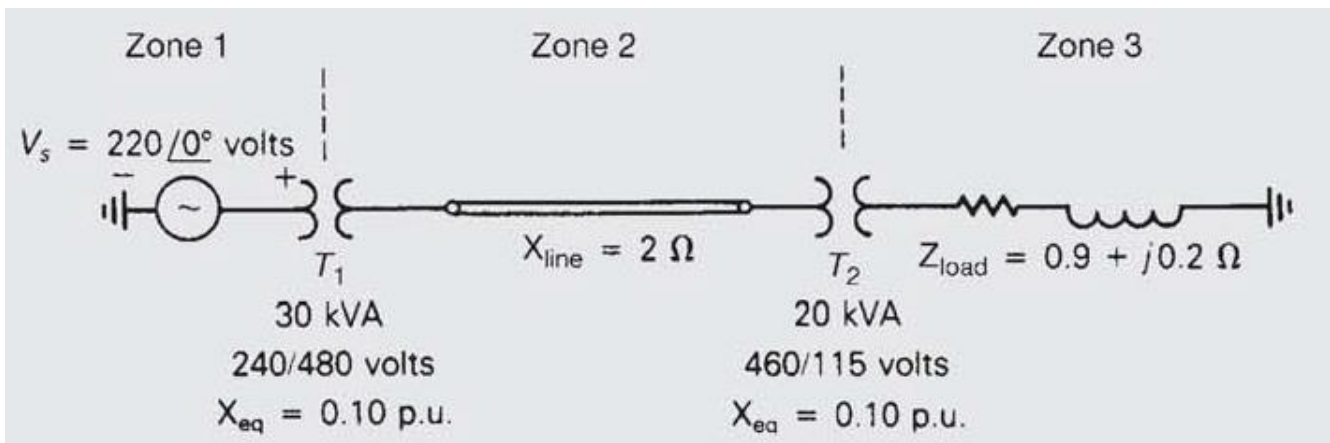
**Load 3:** Is 120 kVA at 0.6 PF leading

If the line-to-neutral voltage at the load end of the line is 2000 V (rms), **determine the magnitude of the line-to-line voltage at the source end of the line.**

**Q2-(30)** For the circuit shown below, convert the voltage sources to equivalent current sources and write nodal equation in matrix format using bus 0 as the reference bus. Do not solve the equation.



**Q3-(35)** Three zones of a single-phase circuit are identified in the figure shown below. The zones are connected by transformer  $T_1$  and  $T_2$ , whose ratings are also shown. Using base values of 30 kVA and 240 V in the zone 1, draw the per-unit circuit and determine the per-unit impedances and the per-unit source voltage. Then calculate the load current both in per-unit and in amperes. Transformer winding resistances and shunt admittance branches are neglected.



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**Solution of EE 465 Midterm Exam1**

**15-11-2018**

1-

On a per-phase basis  $\bar{S}_1 = \frac{1}{3}(150 + j120) = (50 + j40) \text{ kVA}$

$$\therefore \bar{I}_1 = \frac{(50 - j40)10^3}{2000} = (25 - j20) \text{ A}$$

Note: PF Lagging

Load 2: Convert  $\Delta$  into an equivalent Y

$$\bar{Z}_{2Y} = \frac{1}{3}(150 - j48) = (50 - j16) \Omega$$

$$\therefore \bar{I}_2 = \frac{2000 \angle 0^\circ}{50 - j16} = 38.1 \angle 17.74^\circ$$

$$= (36.29 + j11.61) \text{ A}$$

Note: PF Leading

$$\bar{S}_3 \text{ per phase} = \frac{1}{3} [(120 \times 0.6) - j120 \sin(\cos^{-1} 0.6)] = (24 - j32) \text{ kVA}$$

$$\therefore \bar{I}_3 = \frac{(24 + j32)10^3}{2000} = (12 + j16) \text{ A}$$

Note: PF Leading

$$\text{Voltage at the sending end: } \bar{V}_{AN} = 2000 \angle 0^\circ + (73.29 + j7.61)(0.2 + j1.0)$$

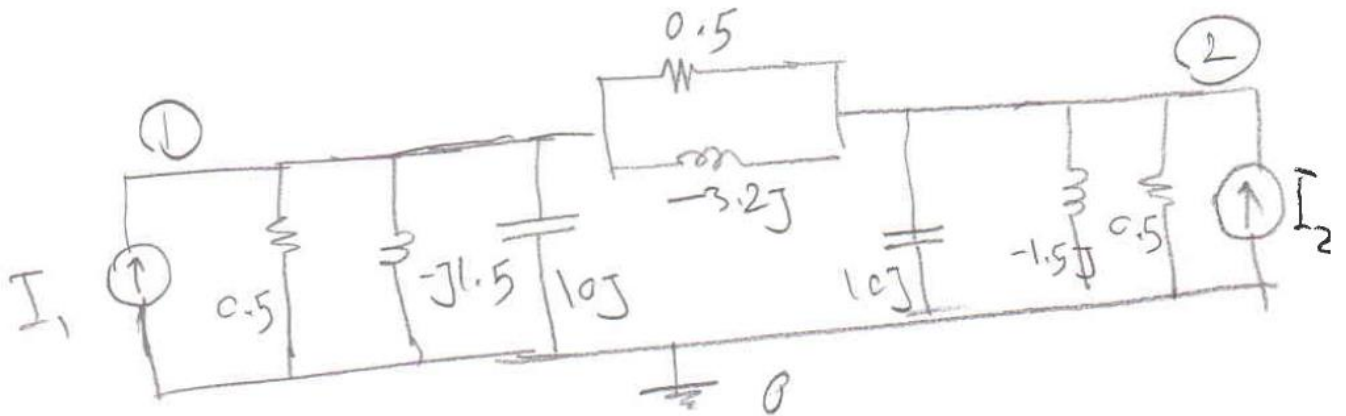
$$= 2007.05 + j74.81 = 2008.44 \angle 2.13^\circ \text{ V}$$

$$\text{Line-to-line voltage magnitude at the sending end} = \sqrt{3}(2008.44) = 3478.62 \text{ V}$$

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2-



$$Y_1 = \frac{1}{Z_1} = \frac{1}{0.2 + j0.6} = 0.5 - j1.5$$

$$Y_2 = \frac{1}{Z_2} = \frac{1}{0.05 + 0.3} = 0.5 - 3.2j$$

$$I_1 = \frac{1.0 \angle 30^\circ}{0.2 + 0.6j} = 1.58 \angle -41.56^\circ$$

$$I_2 = \frac{1.0 \angle 0^\circ}{0.2 + 0.6j} = 1.58 \angle -71.56^\circ$$

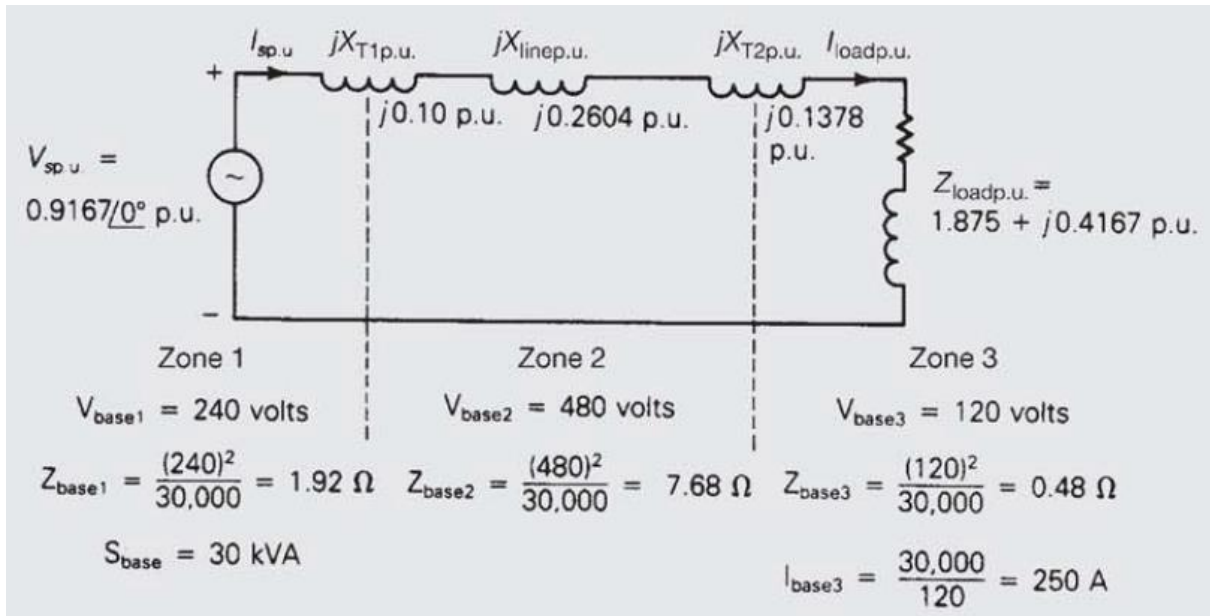
$$Y = \begin{vmatrix} 1.04 + j5.26 & -0.54 + j3.24 \\ -0.54 + j3.24 & 1.04 + j5.26 \end{vmatrix}$$

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$$\begin{vmatrix} 1.04 + j5.26 & -0.54 + j3.24 \\ -0.54 + j3.24 & 1.04 + j5.26 \end{vmatrix} \begin{vmatrix} V_1 \\ V_2 \end{vmatrix} = \begin{vmatrix} 1.58 \angle -41.56 \\ 1.58 \angle -71.56 \end{vmatrix}$$

3-



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First the base values in each zone are determined.  $S_{\text{base}} = 30 \text{ kVA}$  is the same for the entire network. Also,  $V_{\text{base1}} = 240 \text{ volts}$ , as specified for zone 1. When moving across a transformer, the voltage base is changed in proportion to the transformer voltage ratings. Thus,

$$V_{\text{base2}} = \left(\frac{480}{240}\right)(240) = 480 \text{ volts}$$

and

$$V_{\text{base3}} = \left(\frac{115}{460}\right)(480) = 120 \text{ volts}$$

The base impedances in zones 2 and 3 are

$$Z_{\text{base2}} = \frac{V_{\text{base2}}^2}{S_{\text{base}}} = \frac{480^2}{30,000} = 7.86 \ \Omega$$

and

$$Z_{\text{base3}} = \frac{V_{\text{base3}}^2}{S_{\text{base}}} = \frac{120^2}{30,000} = 0.48 \ \Omega$$

and the base current in zone 3 is

$$I_{\text{base3}} = \frac{S_{\text{base}}}{V_{\text{base3}}} = \frac{30,000}{120} = 250 \text{ A}$$

Next, the per-unit circuit impedances are calculated using the system base values. Since  $S_{\text{base}} = 30 \text{ kVA}$  is the same as the kVA rating of transformer  $T_1$ , and  $V_{\text{base1}} = 240 \text{ volts}$  is the same as the voltage rating of the zone 1 side of transformer  $T_1$ , the per-unit leakage reactance of  $T_1$  is the same as its nameplate value,  $X_{T1\text{p.u.}} = 0.1$  per unit. However, the per-unit leakage reactance of transformer  $T_2$  must be converted from its nameplate rating to the system base. Using (3.3.11) and  $V_{\text{base2}} = 480 \text{ volts}$ ,

$$X_{T2\text{p.u.}} = (0.10) \left(\frac{460}{480}\right)^2 \left(\frac{30,000}{20,000}\right) = 0.1378 \text{ per unit}$$

Alternatively, using  $V_{\text{base3}} = 120 \text{ volts}$ ,

$$X_{T2\text{p.u.}} = (0.10) \left(\frac{115}{120}\right)^2 \left(\frac{30,000}{20,000}\right) = 0.1378 \text{ per unit}$$

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which gives the same result. The line, which is located in zone 2, has a per-unit reactance

$$X_{\text{linep.u.}} = \frac{X_{\text{line}}}{Z_{\text{base2}}} = \frac{2}{7.68} = 0.2604 \text{ per unit}$$

and the load, which is located in zone 3, has a per-unit impedance

$$Z_{\text{loadp.u.}} = \frac{Z_{\text{load}}}{Z_{\text{base3}}} = \frac{0.9 + j0.2}{0.48} = 1.875 + j0.4167 \text{ per unit}$$

The per-unit circuit is shown in Figure 3.10(b), where the base values for each zone, per-unit impedances, and the per-unit source voltage are shown. The per-unit load current is then easily calculated from Figure 3.10(b) as follows:

$$\begin{aligned} I_{\text{loadp.u.}} = I_{\text{sp.u.}} &= \frac{V_{\text{sp.u.}}}{j(X_{T1p.u.} + X_{\text{linep.u.}} + X_{T2p.u.}) + Z_{\text{loadp.u.}}} \\ &= \frac{0.9167 \angle 0^\circ}{j(0.10 + 0.2604 + 0.1378) + (1.875 + j0.4167)} \\ &= \frac{0.9167 \angle 0^\circ}{1.875 + j0.9149} = \frac{0.9167 \angle 0^\circ}{2.086 \angle 26.01^\circ} \\ &= 0.4395 \angle -26.01^\circ \text{ per unit} \end{aligned}$$

The actual load current is

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$$I_{\text{load}} = (I_{\text{loadp.u.}})I_{\text{base3}} = (0.4395 \angle -26.01^\circ) (250) = 109.9 \angle -26.01^\circ \text{ A}$$

Note that the per-unit equivalent circuit of Figure 3.10(b) is relatively easy to analyze, since ideal transformer windings have been eliminated by proper selection of base values.

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